

# Quantifying local stiffness and forces in soft biological tissues using droplet optical microcavities

Gregor Pirnat<sup>a,b</sup>, Matevž Marinčič<sup>a,b</sup>, Miha Ravnik<sup>b,a</sup>, and Matjaž Humar<sup>a,b,c</sup>

<sup>a</sup>*Condensed Matter Department, J. Stefan Institute, Jamova 39, SI-1000 Ljubljana, Slovenia*

<sup>b</sup>*Faculty of Mathematics and Physics, University of Ljubljana, Jadranska 19, SI-1000, Ljubljana, Slovenia*

<sup>c</sup>*CENN Nanocenter, Jamova 39, SI-1000 Ljubljana, Slovenia*

*\*E-mail: matjaz.humar@ijs.si*

## Abstract

Mechanical properties of biological tissues fundamentally underlie various biological processes and non-contact, local, and microscopic methods can provide fundamental insights. Here, we present a novel approach for quantifying the local mechanical properties of biological materials at the microscale, based on measuring the spectral shifts of the optical resonances in droplet microcavities. Specifically, the developed method allows for measurements of deformations in dye-doped oil droplets embedded in soft materials or biological tissues with an error of only 1 nm, which in turn enables measurements of anisotropic stress inside tissues as small as a few pN/ $\mu\text{m}^2$ . Furthermore, by applying an external strain, Young's modulus can be measured in the range from 1 Pa to 35 kPa, which covers most human soft tissues. Using multiple droplet microcavities, our approach could enable mapping of stiffness and forces in inhomogeneous soft tissues and could also be applied to in vivo and single-cell experiments. The developed method can potentially lead to new insights into the mechanics of biological tissues.

**Significance Statement:** Due to the importance of mechanical processes in biological organisms there have been a large variety of methods developed to study these processes. However, most of these methods are limited to measuring only one parameter at a time and frequently do not enable measurement inside tissues. By using optical resonances in droplets we are able to measure the deformations of these liquid inclusions to a nanometer accuracy, almost 100 times better than today's state-of-the-art confocal microscopy. This enables quantitative long-term spatial mapping of both the absolute stiffness and forces. Furthermore, the developed approach has the potential to serve as a powerful multimodal probe, enabling simultaneous mechanical mapping, refractive index measurement, and acting as micro barcodes.

**Keywords:** microdroplets, whispering gallery modes, stiffness, biological tissues, liquid inclusions

## 23 Introduction

24 Microscopic mechanical properties and forces are central in diverse materials and material applications, rang-  
25 ing from soft matter [1], microrheology of complex fluids [2] to biological tissues [3], tissue regeneration and  
26 bio-engineering [4]. Distinctly in biology, the forces acting in living organisms play crucial roles in various  
27 developmental, homeostatic, and pathological processes [3, 5], such as cell differentiation and tumor growth.  
28 The role of mechanics is often insufficiently understood, partially because of the limitations of the current mea-  
29 surement techniques. Multiple techniques are used to measure the viscoelastic properties of cells and tissues  
30 and forces acting within them [6, 7], including atomic force microscopy [8], traction force microscopy [9–11],  
31 arrays of micropillars [12, 13], optical tweezers [14] and Brillouin microscopy [15]. Frequently, in these force  
32 measurement techniques, the cells are placed in contact with an artificial material and are spatially isolated to  
33 individual cells or cell monolayers. However, cells require a complex biophysical and biochemical environment  
34 to behave in a truly physiologically realistic manner, which is only achievable in a 3D extracellular matrix or  
35 in vivo. Therefore, a truly non-contact force measurement is needed of cells surrounded only by the biological  
36 environment.

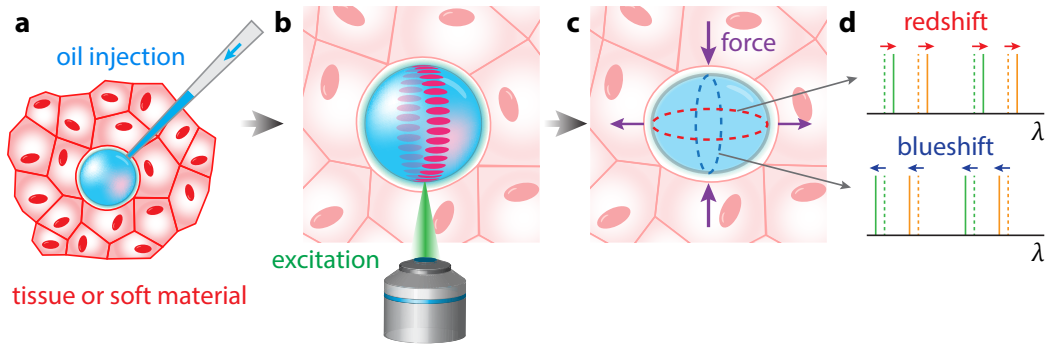
37 Recently, new methods have been developed to measure cell-generated mechanical forces within living tissues  
38 using cell-sized oil microdroplets injected between the cells [16, 17], cell-generated stresses in a microchannel  
39 using emulsion droplets [18] and by spheroid-generated stresses using deformable hydrogel microdroplets [19].  
40 The droplet deformation within a deformed material is governed by the ratio between the interfacial tension and  
41 Young’s modulus. This ratio, also known as the elastocapillary length, is an important parameter, especially  
42 in soft materials and biological tissues. It affects the surface deformation of soft solids [20, 21], fabrication of  
43 solid-liquid composites via 3D printing [22], development of smart materials [23–25], mechanical interaction  
44 between implants and surrounding tissues [26], and governs the morphology of single cells [27].

45 Spherical microresonators that support photonic whispering gallery modes (WGMs) can be used as very  
46 precise sensors and are sensitive to changes in refractive index and shape of the microresonator [28–31]. Specif-  
47 ically, droplet microresonators and microresonators made of soft materials, which easily adapt their shape to  
48 external forces while maintaining smooth surface, have been used as tunable light sources [32, 33], lasers [34–36],  
49 force sensors [37], probes for measuring surface tension [38], as well for single particle detection [39, 40]. How-  
50 ever, there are only a few applications of WGM to study tissue mechanics. For example, anisotropic stress was  
51 measured inside cells [41] and the biological strain of bones was determined [42].

52 In this paper, we demonstrate a WGM-based method for measuring local stiffness and forces in soft and  
53 biological materials via droplet deformations. The introduction of the droplet into tissues is minimally invasive  
54 and after the injection the measurements are non-contact. Our approach enables the measurement of  $\sim 2$   
55 orders of magnitude smaller droplet deformations compared to state-of-the-art confocal microscopy [16]. We  
56 can measure deformations as small as a few nanometers, whereas the measurement error in droplet curvature  
57 measurement by other microscopy is in the order of several 100 nm. Measurement of both anisotropic stress and  
58 Young’s modulus of the material was demonstrated, which is also quite unique compared to other techniques,  
59 where usually only one parameter is measured at a time. We also show that the method is viable in a wide  
60 range of stiffnesses.

## 61 Results and discussion

62 The developed experimental method for measuring the mechanical properties of tissues consists of injecting  
 63 an oil droplet into a tissue, exciting the WGMs within the droplet, collecting the spectra, and analyzing the  
 64 spectral shifts (Figure 1). One or multiple dye-doped oil droplets with sizes of the order of  $10\ \mu\text{m}$  are controllably  
 65 injected into the tissue to a well-controlled position (Figure 1a) or dispersed in a soft material. The maximum  
 66 pressure needed for injection is used to measure the interfacial tension. Whispering gallery modes are excited  
 67 via external illumination and spectra are collected at different positions in the droplet (Figure 1b). Due to forces  
 68 acting within the tissue, the droplet gets deformed from the perfectly spherical shape preferred by the surface  
 69 tension (Figure 1c). By measuring spectral shifts of WGMs circulating in different planes in the droplet (Figure  
 70 1d), the deformation amplitude and direction can be quantified. Finally, combining the measured deformations  
 71 with numerical simulations enables us to relate the droplet size, droplet deformation, Young’s modulus, strain,  
 72 and interfacial tension. In this work, to validate the method, the measurements are first performed in soft  
 73 hydrogels with known mechanical properties and by applying a controlled external strain. The used gelatine  
 74 hydrogel has Young’s modulus of  $1.6\ \text{kPa}$  which is similar to the stiffness of soft biological materials such as  
 75 brain  $1\text{-}10\ \text{kPa}$  [43–45] and fat tissue  $1\text{-}4.5\ \text{kPa}$  [46].

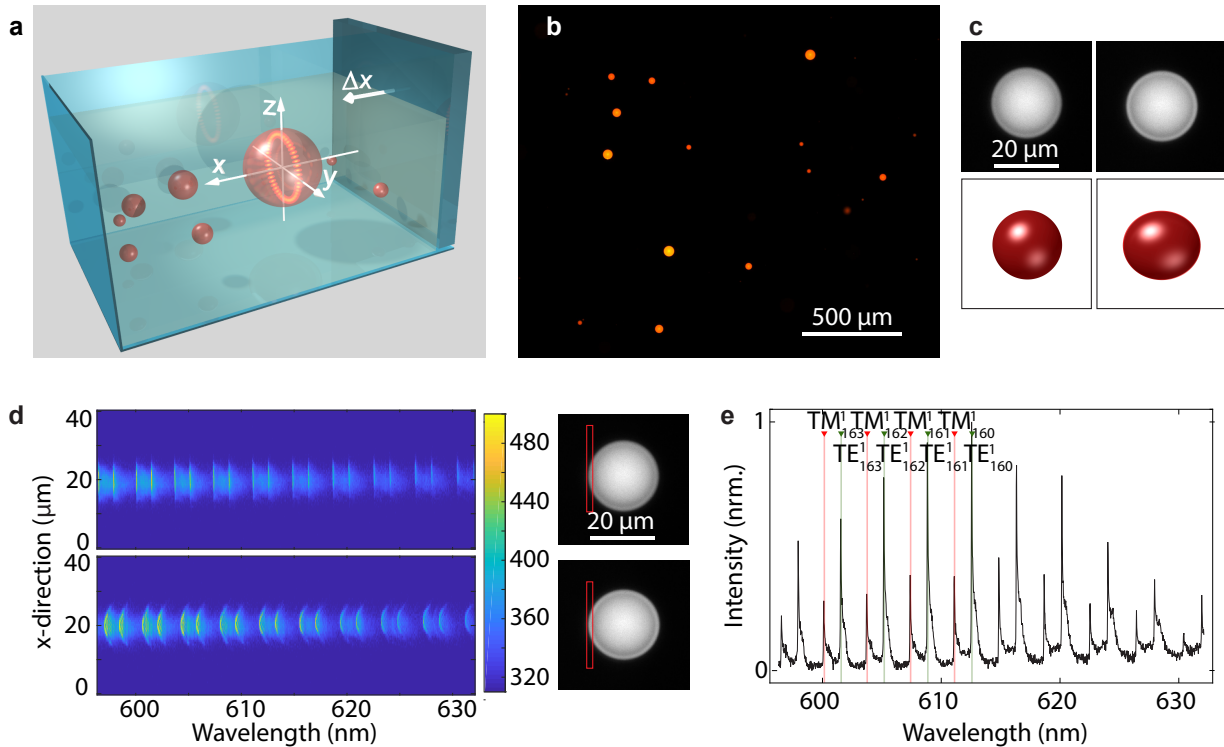


**Figure 1.** Schematic illustration of the experimental workflow. (a) A droplet is injected into the investigated material via a microcapillary. (b) Droplet acts as an optical microcavity when its optical resonances are excited by an external light source. (c) The droplet deforms due to external forces, whereas the interfacial tension resists droplet deformation. (d) The measured WGM wavelengths are dependent on the optical path length: any droplet deformation results in a redshift or a blueshift depending on whether the circumference in that plane increases or decreases, respectively.

### 76 Droplet deformation in hydrogel

77 The experimental setup consisted of a rectangular glass container filled with a dispersion of fluorescent dye-doped  
 78 oil microdroplets ( $n = 1.62$ ) in a gelatin-based hydrogel (Figure 2a). The hydrogel containing the droplets was  
 79 deformed by a movable wall, connected to a linear motorized stage. The sample was compressed or stretched in  
 80 the  $x$ -direction. In the  $y$ -direction the hydrogel was restricted by the walls of the container. In  $z$ -direction the  
 81 bottom was closed by the glass slide, while the top surface of the hydrogel was free to move up and down. The  
 82 droplet dispersion was prepared in two stages, as described in the methods section so that the polydispersed  
 83 microdroplets were situated in a single horizontal plane (Figure 2b). By positioning the droplets in a single plane

84 all droplets are in focus, which enables all their positions and shapes to be tracked simultaneously. Furthermore,  
 85 this reduces the overall number of oil droplets in the hydrogel, thus minimizing their effect on Young's modulus  
 86 of the composite material [47]. Alternatively, the droplets can also be injected via microcapillary to a specific  
 87 position in a three-dimensional volume.

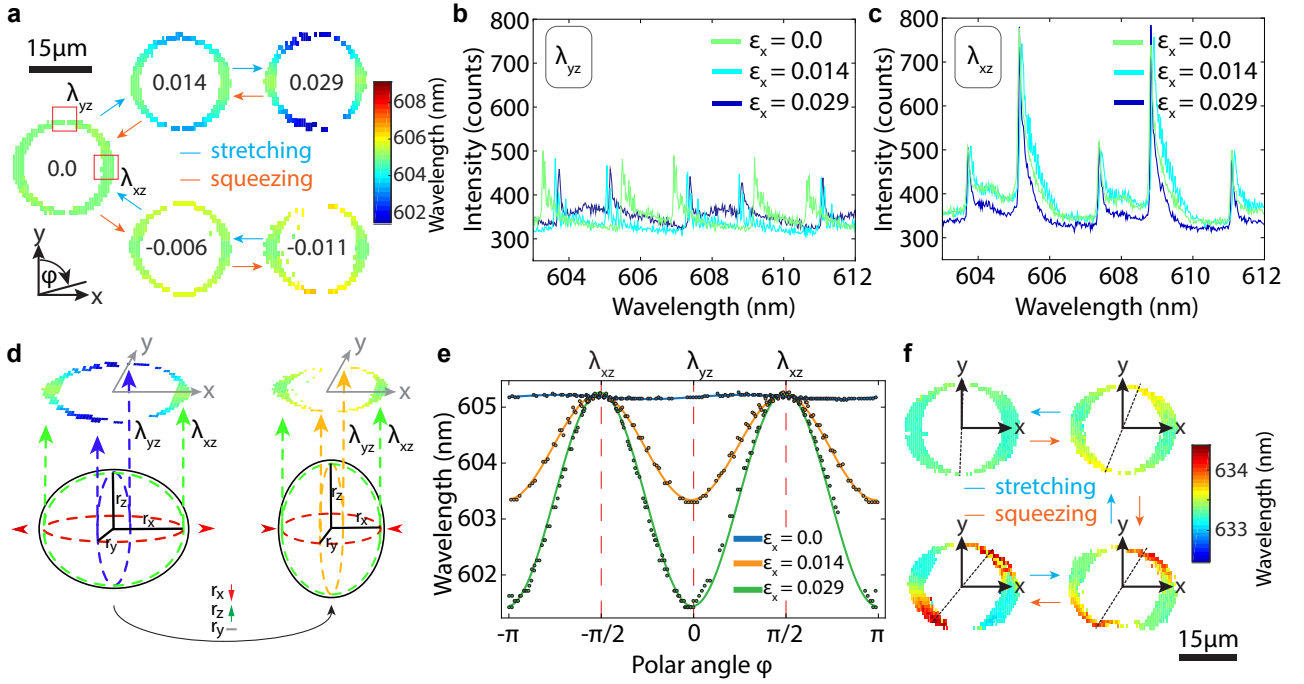


**Figure 2.** Droplet deformation in a hydrogel. (a) Schematic illustration of the experimental setup. A wall moves in  $x$ -direction deforming the hydrogel, which contains oil droplets. (b) Fluorescence image of microdroplets which are randomly distributed within a single plane in the hydrogel. (c) Droplet before induced deformation (left) and deformed droplet (right) at 0 and 2.8% deformation of the hydrogel, with a schematic of the droplet's shape with exaggerated deformation ( $20\times$  magnified) to assist visualization of the measurement concept. (d) Spatially resolved spectra along the spectrometer slit (red rectangle) positioned across a single droplet without induced deformation (top) and a deformed droplet (bottom). (e) Typical spectrum at a single point on the droplet's rim without induced deformation.

88 The wall was moved in steps of typically  $50 \mu\text{m}$ . At each step two measurements were taken: a fluorescence  
 89 image in a wider field of view and a hyperspectral fluorescence image of the droplet of interest. The fluorescence  
 90 image containing multiple droplets in the surroundings of the droplet of interest was used to determine the  
 91 local strain of the hydrogel (Supplementary Figure 1). This was achieved by tracking the relative positions  
 92 of the droplets with a  $0.5 \mu\text{m}$  error. Instead of using multiple droplets, additional small fluorescent particles  
 93 could be used to measure local strain with a higher spatial resolution, as it is usually done in traction force  
 94 microscopy [48]. For the hydrogel far from any wall of the container, the  $y$ -component of the measured strain  
 95 was negligible, whereas the  $x$ -component was in agreement with the displacement of the movable wall. At the  
 96 largest applied strain of 4% the droplet deformations were too small to be resolved by imaging alone (Figure  
 97 2c); therefore, WGM measurements were needed and applied for further investigation.

## 98 Whispering gallery mode measurements

99 The hyperspectral scans were first made for samples without induced deformation by the movable wall (Figure  
 100 2d-top). In this case, the maximum WGMs shift along the droplet's rim is only  $\sim 0.05$  nm (Supplementary  
 101 Figure 2). In this state, already higher order modes can also be observed all around the droplet's rim as  
 102 asymmetrically broadened peaks (Figure 2e), which indicates that the droplet is somewhat compressed in the  
 103  $z$ -direction. However, since this semi-axis  $r_z$  is common for all modes that radiate in the  $z$ -direction,  $r_z$  is less  
 104 relevant and only contributes a small error to the final result (Supplementary Information). The droplet size  
 105 is then determined by fitting the TE and TM modes [49] to the first-order azimuthal WGMs and verified with  
 106 the camera image of the droplet.



**Figure 3.** Experimental measurements of droplet deformation via shifts of WGMs. **(a)** Measured wavelength shift of a single WGM peak at different points on the rim of the droplet. The hydrogel surrounding the droplet was stretched up to a strain of  $\epsilon = 0.029$  and squeezed up to  $\epsilon = -0.011$ . The top row represents droplet extension and the bottom row droplet compression. **(b)** Droplet spectra from  $xz$ - and **(c)**  $yz$ -plane, at different strains. **(d)** Geometry of the droplet deformation is represented by the ellipsoid with semi-axes ( $r_x$ ,  $r_y$  and  $r_z$ ), planes of the WGMs circulation (green, blue and orange dashed lines) and the WGM wavelengths corresponding to these planes ( $\lambda_{yz}$  and  $\lambda_{xz}$ ). Red dashed lines correspond to the droplet circumference as observed through the microscope. The superimposed wavelength shifts at the top belong to the same droplet as figures **a-e**. **(e)** Wavelength shifts from **a** (top row) fitted to an ellipse in polar coordinates at three different strains. **(f)** WGM shifts at different points on the rim of a diagonally deformed droplet.

107 The hydrogel was deformed which caused a local strain  $\epsilon$ . This deformation led to different shifts in the  
 108 WGMs around the droplet's rim (Figure 3a). The shifts are also very distinctly visible in a single-line scan when  
 109 the spectrometer slit is aligned with the edge of the droplet. The shifts appear as crescent shapes (Figure 2d).  
 110 When the droplet is stretched the WGMs along the  $y$ -direction ( $\lambda_{yz}$ ) blueshift (Figure 3b), while conversely  
 111 when the droplet is compressed the modes redshift. The modes in the  $x$ -direction ( $\lambda_{xz}$ ) (Figure 3c) do not shift

112 in either stretching or compressing. This is expected for the geometry in our experiment, where the external  
 113 strain deforms the hydrogel in the  $xz$  plane but not in the  $y$  direction. In this geometry, all three axes of the  
 114 ellipsoid ( $r_x$ ,  $r_y$ , and  $r_z$ ) can be determined from the spectral shifts on a single hyperspectral image. The relation  
 115 between the ellipsoid shape and spectral shifts is given in the Supplementary Information. To determine the  
 116 droplet aspect ratio in the  $xy$ -plane  $r_x/r_y$  only the measurements of the minimum and maximum wavelength  
 117 shifts are required. However, because a hyperspectral scan is performed, all spectra along the circumference  
 118 can be used for a more precise analysis (Figure 3d and e), improving the measurement of both the magnitude  
 119 and the direction of the deformation. Finally, this also enables us to determine if the deformation is indeed of  
 120 an ellipsoid shape. Figure 3e shows jointly the three results by plotting the wavelength of a single optical mode  
 121 as a function of the polar angle  $\lambda(\varphi)$  around the droplet rim. The measured data agrees well with the equation  
 122 of an ellipse, meaning that the droplet is deformed into an ellipsoid shape, at least for small external strains.  
 123 The simulations also confirm the ellipsoid shape.

124 The error in measuring the droplet deformation was determined as the fitting error of the amplitude of the  
 125 ellipsoid curve in Figure 3e. The error determined in this way includes the contributions from the noise, the  
 126 spectral resolution of the spectrometer, and any deviations from an elliptical shape. The fitting error translates  
 127 to a distinguishable relative change in the droplet's semi-axis of about 1 nm.

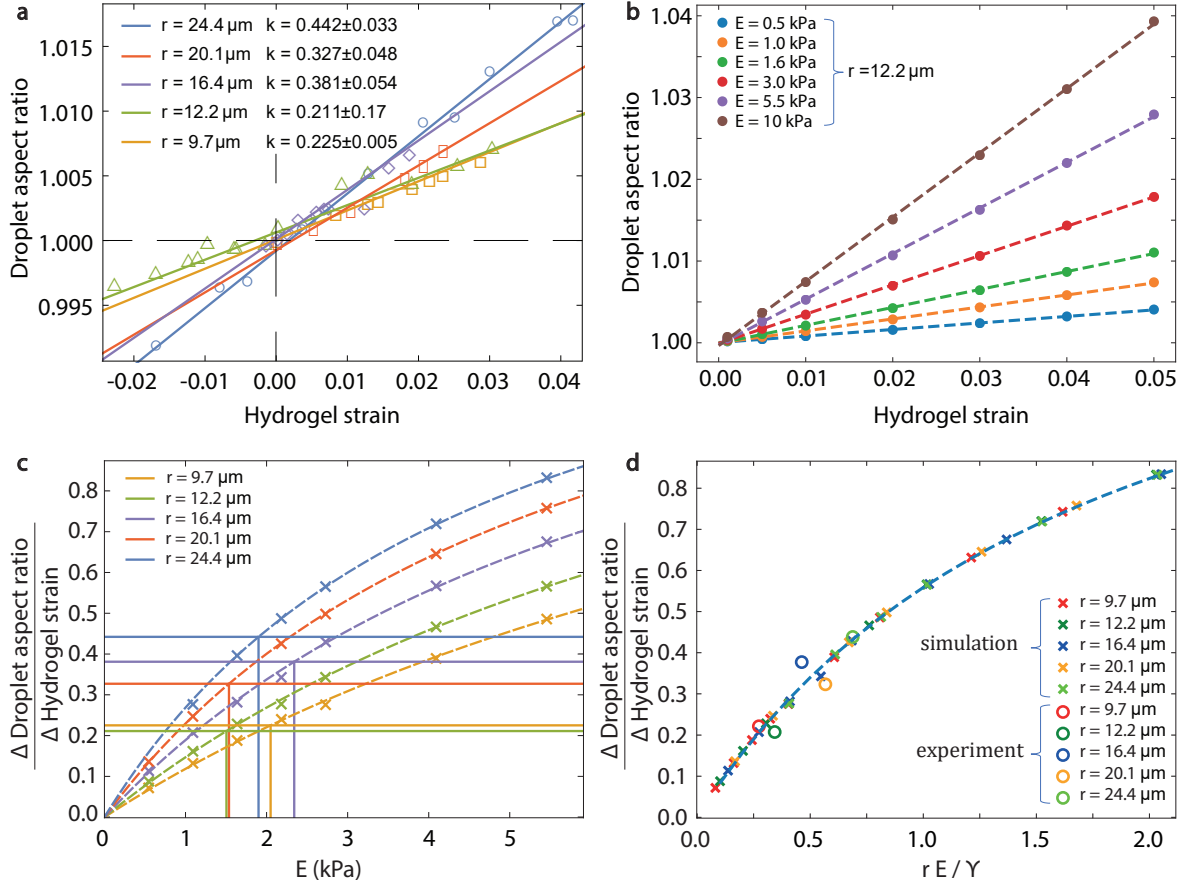
128 From the shift of the  $\lambda(\varphi)$  curve the deformation direction can be determined as well. While in the first  
 129 example (Figure 3e) the deformation is exactly along the axis, the droplets near the container side wall experience  
 130 a diagonal deformation (Figure 3f). The deformation angle increases from  $2^\circ$  to  $35^\circ$  when the external strain is  
 131 increased.

### 132 **Determination of Young's modulus**

133 The deformation of liquid inclusions in a cubic sample of the elastic material (hydrogel) was simulated to corroborate  
 134 the experimental results and to relate them to the mechanic properties. The free energy minimization was  
 135 implemented with finite elements method (FEM). The semi-axes and the droplet aspect ratio are determined  
 136 by fitting an ellipse to the cross-section of the droplet, confirming the tri-axial ellipsoidal shape as described in  
 137 the previous section. The details about the simulation are discussed in the Methods section and Supplementary  
 138 Information.

139 The experimental data showing the dependence of droplet aspect ratio  $\eta = r_x/r_y$  to hydrogel strain  $\epsilon$   
 140 was fitted with a linear function to determine the slope coefficients  $k = \Delta\eta/\Delta\epsilon$  which vary for different sized  
 141 droplets (Figure 4a). The droplet aspect ratio  $\eta$  is calculated from the experimentally measured wavelength  
 142 shifts, as discussed in the previous section. Due to the experimental error in hydrogel strain measurements  
 143 (Supplementary Figure 3) the reference state without induced deformation is not precisely determined, which  
 144 is why the linear fits in experimental data can have nonzero droplet deformation at zero strain. The occasional  
 145 pre-strain as measured by WGMs of the droplets without deliberately induced deformation was only observed  
 146 in the  $x$ -direction and is not problematic since only the slope of the linear fit  $k$  is used in our measurement  
 147 technique, and does not change in the case of strain offset.

148 The linear dependency is reproduced in the simulation by increasing the strain in the same range as in  
 149 the experiments (Figure 4b). In the simulations, the interfacial tension  $\gamma$  and the droplet size  $r$  are fixed and  
 150 Young's modulus  $E$  is varied. As expected, a stiffer hydrogel will increase the droplet aspect ratio at the same



**Figure 4.** Data analysis and material parameter extraction. **(a)** Experimental measurements of deformation of droplets with different radii  $r$  as the external hydrogel strain is increased. **(b)** Droplet aspect ratio  $\eta = r_x/r_y$  with respect to the average hydrogel strain  $\epsilon$  far from the droplet for simulations of one droplet with radius  $r = 12.2 \mu\text{m}$  and different elastic moduli  $E$ . The slope of the linear fit  $k = \Delta\eta/\Delta\epsilon$  is calculated for both experimental and simulation results and plotted in **(c,d)**. **(c)** Simulated results for varying elastic moduli  $E$  and experimentally measured droplet radii  $r$  are represented by crosses and connected with a dashed line. Experimental measurements corresponding to the same droplet sizes are shown as horizontal lines with matching colors. The intersection of the horizontal lines and curved lines for each specific droplet radius indicates the measured Young's modulus  $E$ . **(d)** Experimental and simulated data on the same curve, and plotted against the dimensionless quantity  $rE/\gamma$ , which gives the final results  $E = 1800 \text{ Pa}$  and  $\gamma = 65 \text{ mN/m}$ .

151 hydrogel strain, as the effect of interfacial tension becomes less important.

152 The simulations were repeated for the same droplet radii, as used in the experiments. The slopes of the  
 153 linear fits  $k$  are used to relate the simulations to the experiments. The slope  $k$  increases with Young's modulus  
 154  $E$  (Figure 4c). Larger droplets deform more at the same material parameters. Each experimental measurement  
 155 for a different droplet radius is represented by a horizontal line (Figure 4c) and fits a specific Young's modulus.  
 156 The average across five experimental measurements gives the elastocapillary length  $\gamma/E = 35.3 \mu\text{m}$ .

157 To determine Young's modulus from the elastocapillary length, the interfacial tension has to be known  
 158 or measured. Because the absorption of surfactant molecules on the oil droplet can significantly change the  
 159 interfacial tension, it is best to measure it locally. For this reason the maximum bubble pressure tensiometry  
 160 method [50, 51] was used. A microcapillary is inserted into the material and pressure is gradually increased

161 until an oil droplet is generated. The interfacial tension is calculated by the Laplace equation  $\gamma = p_{\max}/D$ ,  
162 where  $p_{\max}$  is the pressure inside the microcapillary needed to create the droplet and  $D$  is the microcapillary  
163 inner diameter. Because the inner microcapillary diameter of  $0.5\ \mu\text{m}$  is much smaller than the elastocapillary  
164 length  $35\ \mu\text{m}$ , the contribution of elasticity can be neglected. From the maximum pressure of  $1350 \pm 100\ \text{mbar}$   
165 the interfacial tension was measured to be  $65 \pm 5\ \text{mN/m}$ . Notably, this method for locally measuring the  
166 interfacial tension between the droplet and the embedding material comes with the advantage of more accurate  
167 measurements, as the actual value can vary even inside the tissue. From our measurements, the variation inside  
168 the gelatin hydrogel was about 10%, and inside tissues was about 20%.

169 Taking into account the measured elastocapillary length  $\gamma/E$  the final result for Young's modulus of the  
170 hydrogel averaged over 5 droplets is  $E = 1800 \pm 300\ \text{Pa}$ . This matches very well with the value measured by  
171 the indentation ( $E = 1700 \pm 600\ \text{Pa}$ ). The error of the measured stiffness both with droplets and with the  
172 indentation is mainly due to the variability of the samples, as evident also in other studies [52]. Here, it is worth  
173 pointing out that the optical resonances were essential for measuring Young's modulus because the droplet  
174 deformation due to external strain has to be measured with an error of less than 10 nm, which is too small for  
175 optical imaging.

176 The results can also be represented together on a single curve (Figure 4d) by plotting the slope  $k$  as a function  
177 of a dimensionless quantity  $rE/\gamma$ . This quantity is the key scaling parameter and the solutions for different  
178 combinations of parameters  $E$ ,  $\gamma$ , and  $r$  fall on the same curve, in line with known literature on liquid inclusions  
179 in soft materials [47]. In our experiment, as is the case with  $\mu\text{m}$ -sized droplets in many biologically relevant  
180 materials, both interfacial energy and elastic strain energy contribution are equally important ( $rE/\gamma \sim 1$ ),  
181 which enables the measurement of the material parameters through this method, specifically the elastocapillary  
182 length  $\gamma/E$ .

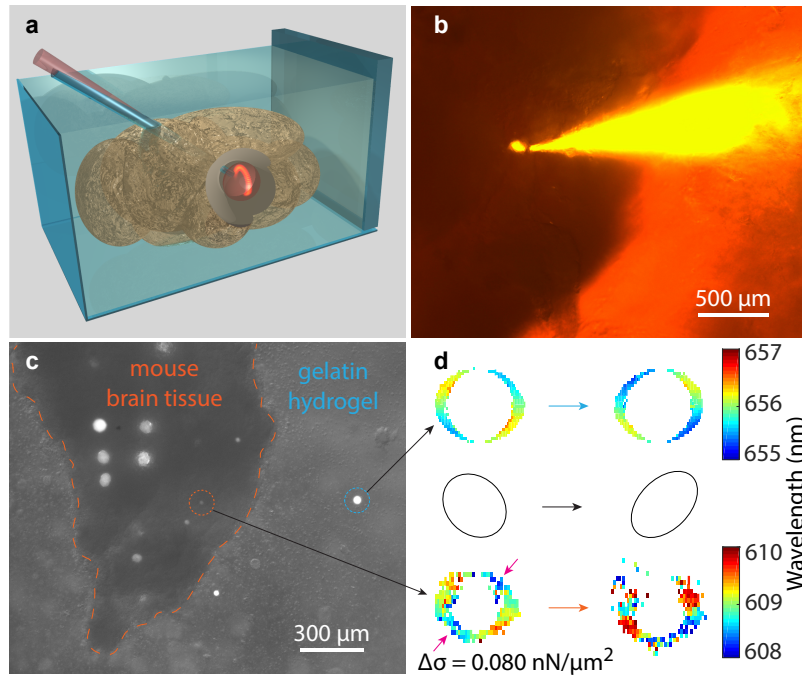
183 The observed dependence of the droplet aspect ratio on material parameters eventually reaches Eshelby's  
184 limit for liquid inclusion without interfacial tension [53], when all liquid inclusions deform at the same rate  
185 regardless of their size  $r$ , which is seen in Figure 4d as the profile levels off for larger droplets  $r \gg \gamma/E$ .  
186 Actually, this sets the upper limit for measuring elastocapillary length  $\gamma/E$ , when the effect of surface tension  
187 becomes negligible and the measurement of Young's modulus is not possible. However, this limit can be used  
188 for measuring material strain directly through WGM measurements, as the dependence between droplet aspect  
189 ratio and material strain is linear. Material strain can be measured directly from WGM measurements also  
190 outside this limit once the material parameters  $E$  and  $\gamma$  are known.

191 Therefore, to measure materials with a high Young's modulus ( $>10\ \text{kPa}$ ), small droplets ( $<20\ \mu\text{m}$ ) with high  
192 interfacial tension ( $>30\ \text{mN/m}$ ) should be used. Conversely, for soft materials large droplets and low interfacial  
193 tension are required. Using these parameters in an experimentally achievable range and taking into account  
194 the error of the deformation measurement via WGMs, the measurable Young's modulus range is 1-35 000 Pa  
195 (Supplementary Information). Importantly, note that this range spans across most soft human tissues, from  
196 mucus 10 Pa to a part of the muscle tissue 5-150 kPa, however, it is out of range for stiffer tissues such as  
197 epidermis, heart muscle and some tumors [54].



198 **Biological tissues**

199 After validation using hydrogels, the method was applied to biological tissues. Small pieces of mouse brain tissue  
 200 ( $\sim 1 \text{ mm}^3$ ) were embedded in the same gelatin hydrogel as used above. A glass microcapillary with a  $0.5 \mu\text{m}$  inner  
 201 diameter was used to inject oil droplets into the brain gray matter and the surrounding hydrogel (Figure 5a-c).  
 202 The droplets were injected close to the interface between the brain and hydrogel (up to  $\sim 50 \mu\text{m}$ ) so that they  
 203 could be easily imaged. The use of microcapillary makes the method minimally invasive and non-contact after  
 204 the droplets have been injected. The droplets could also be premixed with the precursor cells when studying for  
 205 example organoid growth in vitro. In this case, the method would be completely non-invasive. The hydrogel,  
 206 which contained the brain tissue, was deformed by a movable container wall. The spectra from droplets in the  
 207 brain tissue as well as in the hydrogel were measured before and after the external deformation was applied  
 208 (Figure 5d). Initially, the droplets were already deformed. From the deformation, the initial internal stress  
 209 (force) acting within the tissue was determined by using the Laplace equation [16]. The anisotropic stress in the  
 210 plane perpendicular to the observation is measured to be  $\Delta\sigma = 0.080 \pm 0.003 \text{ nN}/\mu\text{m}^2$ . The smallest anisotropic  
 211 stress that can be measured is limited by the smallest measurable droplet deformation, the size of the droplet,  
 212 and the interfacial tension. For a typical case, it is in the order of a few  $\text{pN}/\mu\text{m}^2$ .



**Figure 5.** Measurement of stiffness and forces in brain tissue. (a) Schematic illustration of the experimental setup for measuring mechanics of mouse brain tissue, where an oil droplet is injected into the brain tissue contained within gelatin hydrogel. (b) Fluorescence image of a microcapillary at the moment of separation from the generated droplet in the brain tissue. (c) Multiple droplets at various positions in the brain tissue as well as in the surrounding gelatin hydrogel. (d) Wavelength shifts of a single WGM peak for the droplets in gelatin (top) and in brain tissue (bottom).

213 In order to measure Young's modulus of the brain tissue, an external deformation was applied to the brain  
 214 tissue embedded inside the hydrogel. In general, the tissue can have a different stiffness than the hydrogel,  
 215 therefore the strain in the tissue can be different than in the hydrogel. For that reason, the local strain was  
 216 measured by the change in the relative positions of multiple droplets injected into the brain as well as other

217 visual reference points of the brain tissue. Interfacial tension of oil droplets in brain tissue was measured by the  
218 maximum bubble pressure tensiometry method. The maximum pressure was approximately two times smaller  
219 than in the hydrogel while using the same microcapillary, giving an interfacial tension of  $35 \pm 3$  mN/m. A lower  
220 interfacial tension compared to just gelatine is expected due to the presence of various surfactants in tissues.

221 The WGM shifts caused by the applied external strain indicate that both the direction and the magnitude  
222 of the droplet deformation changed (Figure 5d). From this change, the measured strain and the interfacial  
223 tension, Young's modulus was measured to be  $4.9 \pm 1$  kPa for the droplet in Figure 5c. This is comparable to  
224 the values for mouse brain from the literature 1-10 kPa [43–45]. Because multiple droplets were embedded into  
225 the tissue and the surrounding hydrogel (Figure 5c), a distinct difference in Young's modulus at both positions  
226 was measured. With multiple droplets, Young's modulus could even be mapped in 3D, although limited by the  
227 concentration of the embedded droplets.

228 For practical applications, such as in vivo measurements, the maximum depth in the tissue where the method  
229 still works is very important. Because the spectral imaging is very similar to a regular confocal microscope,  
230 the penetration depth should also be very similar. To test the depth of penetration, imaging through optical  
231 phantoms with known scattering properties was performed. The properties of the phantoms were measured  
232 by an integrating sphere. At an optical thickness of 6 mean free paths the shape of the droplet could be  
233 easily determined by measuring the spectral shifts. The maximum depth was estimated to be approximately  
234 10 mean free paths, which is also the commonly acknowledged depth limit of imaging techniques using ballistic  
235 photons [55]. The 6 and 10 mean free paths correspond to 400  $\mu$ m and 670  $\mu$ m in the mammalian cerebral cortex,  
236 respectively. By using a pulsed laser it was possible to measure the WGM spectra up to a depth of 20 mean  
237 free paths, corresponding to 1300  $\mu$ m in the mammalian cerebral cortex. At this depth, it was not possible to  
238 capture a hyperspectral scan, but still mode splitting was observed (Supplementary Figure 4), which may also  
239 be used to estimate the droplet deformation.

240 We have also recently demonstrated that the microcavity spectrum can be detected from as deep as 3.5  
241 transport lengths [56], which corresponds to 3.5 mm in the mammalian cerebral cortex at a wavelength of 620  
242 nm. The potential use of two-photon excitation [57, 58] would improve the maximum depth even further.

## 243 **Further directions**

244 In this study, a single hyperspectral image of the droplet is used to determine the droplet shape and the  
245 anisotropic stress in the plane perpendicular to the observer direction. However, using hyperspectral images from  
246 multiple directions, the deformation along all three semi-axes of the ellipsoid and its orientation could be uniquely  
247 determined for an arbitrary deformation. This would be useful in more complex biological environments, where  
248 internal strains are less homogeneous.

249 In general, the new method is expected to work for all the cases where confocal microscopy is applicable.  
250 There is a broad selection of tools available for confocal microscopy in vivo, such as immobilization devices and  
251 cranial windows. The most limiting factor is the light penetration, which is the same limitation as for confocal  
252 microscopy. However it is still useful for smaller organisms and embryos; for example, imaging of droplet shapes  
253 was shown in live embryos [16].

254 Beyond the demonstrated applications, the developed method and WGM droplet microcavities could be  
255 simultaneously employed as mechanical sensors, refractive index sensors, and spectral barcodes. While our

256 method does not require prior knowledge of the refractive index for either the droplet or the external medium,  
257 if one refractive index is known, then both the diameter and the other refractive index can be determined by  
258 fitting the WGMs. [49]. Because the droplet refractive index is known, the external refractive index can be  
259 measured. In this way for example the water content of hydrogels and biological materials could be measured,  
260 which is in turn also important for their mechanical properties. Further, WGM microcavities have been shown  
261 to be a very powerful way of barcoding, especially for cell tagging and tracking [59–61]. For spherical cavities,  
262 the diameter is used as the unique identifier. For droplets that can deform, alternatively, the volume could be  
263 used as the unique identifier.

## 264 **Conclusions**

265 We have demonstrated that droplets supporting WGMs are an exceptionally precise and versatile method for  
266 studying biomechanical forces and stiffness at the microscale. Our method offers significant advantages for  
267 investigating the mechanical properties of biological tissues.

268 Firstly, our method allows for long-term measurements of mechanical properties in 3D biological tissues  
269 without requiring significant contact with an artificial material, as is the case with most other force measure-  
270 ment methods such as AFM and traction force microscopy. This makes it possible to obtain measurements of  
271 mechanical properties in biological tissues over extended periods of time. Secondly, our method by combining  
272 maximum bubble pressure tensiometry and droplet deformation measurements enables simultaneous measure-  
273 ment of Young’s modulus, magnitude and direction of strain, interfacial tension of oil droplets embedded in  
274 tissue, as well as the intrinsic internal anisotropic stress (force) within the tissues. To the best of our knowl-  
275 edge, no other technique can measure all of these quantities simultaneously. Thirdly, absolute values of all of  
276 the quantities mentioned above can be measured without making assumptions about the tissue. Our method  
277 requires only the inner diameter of the microcapillary used for the injection to be known in advance and no ad-  
278 ditional measurements outside this setup are needed. Fourthly, by injecting multiple droplets our method allows  
279 for the mechanical properties of tissues to be measured at different positions across the tissues. The droplets  
280 used here are of cell size ( $\sim 10\ \mu\text{m}$ ), therefore enabling very localized measurements and in the future will allow  
281 for 3D mapping of mechanical properties and measurement within single cells [41]. Fifthly, the new method  
282 enables the measurement of Young’s modulus in a very wide range of values from 1 Pa to 35 kPa. Notably, the  
283 determination of Young’s modulus of very soft materials ( $<1\ \text{kPa}$ ) is difficult [46].

284 Overall, our droplet microcavity method provides an innovative approach for measuring the stiffness and  
285 forces in biological tissues with high accuracy and versatility. The ability to jointly measure a quite unique set  
286 of mechanical parameters can significantly complement other established methods and has high potential in the  
287 field of biomechanics by enabling the study of a wide range of mechanical aspects of biological tissues, both in  
288 vitro and in vivo.

## 289 **Materials and Methods**

### 290 **Sample preparation**

291 Gelatin from porcine skin (gel strength 90-110 g, Sigma Aldrich, Germany) was dissolved in PBS (phosphate  
292 buffered saline) at a concentration of 8.5 %w/w. The solution was briefly elevated to 90°C and then filtered

293 by 0.2  $\mu\text{m}$  syringe filter. Polyphenyl ether oil (Santolubes, USA, SL5262,  $n = 1.62$ ) doped with 0.1 %w/w  
294 fluorescent dye (pyromethene 597, Exciton, USA) was mechanically stirred into the liquid gelatin to form  
295 polydispersed droplets. SL5262 oil is also compatible with standard lipophilic biocompatible dyes [62], which  
296 would be more suitable for live samples. To get the brain tissue, the mouse head was decapitated, and the skin  
297 from the upper part of the head was removed, followed by the removal of the skull and brain with a scalpel and  
298 tweezers. Only tissues of mice euthanized for other ethically approved studies were used.

299 A rectangular container with dimensions 21.6 mm  $\times$  23.8 mm (2-well  $\mu$ -chamber, Ibidi, Germany) was used.  
300 A glass slide fixed to a motorized linear stage (MFA-CC, Newport) was inserted vertically into the container.  
301 First a 1.5 mm thick hydrogel layer without dispersed microdroplets was poured into the container and left to  
302 solidify. A gelatin solution with dispersed microdroplets at 27°C was added, to a combined total height of 3 mm.  
303 The sample was shut air-tight with para-film foil, and in the neighboring chamber, a sponge soaked with water  
304 was put to prevent the hydrogel from drying. After the gelation of the hydrogel, the sample was left to rest for  
305 another  $\sim 4$  hours before measurements. Samples containing mouse brain tissue were prepared using the same  
306 method and experimental setup. Instead of hydrogel containing oil droplets, it contained pieces of mouse brain  
307 tissue. Oil droplets were injected afterward using a 0.5  $\mu\text{m}$  inner diameter microcapillaries. The microcapillary  
308 moved through soft gelatin with ease, and droplet creation inside the gelatin and brain tissue was performed  
309 by applying pressure to the oil inside the microcapillary. Typically, the minimum pressure needed to inject  
310 droplets into gelatin and the brain was 1300 mbar and 750 mbar, respectively.

### 311 **Optical setup**

312 Microdroplets were illuminated by green LED (CoolLED, UK, pE-300, 0.5-20 mW) through a 20  $\times$  objective  
313 (0.45 NA). The fluorescent light was collected through the same objective and sent simultaneously to an imaging  
314 spectrometer (Andor, UK, Shamrock 500i) with 10  $\mu\text{m}$  input slit width and a grating of 1200 lines per millimeter.  
315 The effective collection NA was 0.23 due to using the microscope's internal magnification. Fluorescence image  
316 of a wider field of view was imaged beforehand with a digital camera (Andor, UK, sCMOS Zyla 4.2) with a  
317 4  $\times$  objective. To capture a hyperspectral image, each droplet was scanned with the push-broom technique.  
318 This involves capturing spatially resolved spectra along the spectrometer slit and moving the sample in steps  
319 to capture spectra for each point of the image. The spatial pixel resolution of the hyperspectral image was  
320  $\sim 0.5 \times 0.5 \mu\text{m}^2$ . For faster scanning, the scan was made with steps of 1  $\mu\text{m}$ . The motorized microscope stage  
321 was used to automatically travel between positions of individual droplets to perform the hyperspectral imaging  
322 on each of them.

### 323 **Young's modulus**

324 As an independent measurement, Young's modulus of the hydrogel was measured with the indentation method  
325 using the Hertz model [63]. A 1 mm diameter glass capillary with spherical tip shape was used to probe  
326 20 mm  $\times$  20 mm  $\times$  10 mm hydrogel sample at room temperature. Indentation depth was imaged with a camera  
327 and force measurement was performed by Metler Toledo balance with 0.01 mN accuracy.

## 328 **Simulations**

329 Simulations were implemented with a finite elements method using an open source python library FEniCS [64].  
330 An open-source 3D finite element mesh generator Gmsh [65] was used to generate a non-uniform 3D mesh  
331 (Supplementary Figure 5). Typically, the size of the simulation box was  $10\times$  larger than the diameter of the  
332 droplet so that the effects of a finite simulation box are negligible. To reproduce the experiment, a cube of elastic  
333 material (hydrogel) was simulated with an initially spherical liquid inclusion, which represents a section of the  
334 hydrogel around a single inclusion (Figure 2a). The external hydrogel strain is implemented by the Dirichlet  
335 boundary condition for the strain at the boundary surfaces. The relaxed structure is numerically calculated by  
336 minimization of total free energy using Newton’s iterative method. The total free energy consists of the linear  
337 elastic free energy of the hydrogel and the interfacial tension free energy term, while the incompressibility of  
338 the liquid inclusion was taken into account by a constraint on the deformation at the droplet surface using the  
339 method of Lagrange multipliers. The detailed mathematical formulation of the problem is in the Supplementary  
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## 346 **Data Availability Statement**

347 The data that support the findings of this study are available from the corresponding author upon reasonable  
348 request.

## 349 **Author contributions**

350 M.H. and M.R. designed research; G.P. and M.M. performed research; G.P. and M.M. analyzed data; G.P.,  
351 M.M., M.R. and M.H. wrote the paper.

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